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**A METHOD FOR ESTIMATING THE  
ROLLING MOMENT DUE TO SPIN RATE  
FOR ARBITRARY PLANFORM WINGS**

**FOR REFERENCE**

NOT TO BE TAKEN FROM THIS ROOM

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# A METHOD FOR ESTIMATING THE ROLLING MOMENT DUE TO SPIN RATE FOR ARBITRARY PLANFORM WINGS

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## ABSTRACT

The application of aerodynamic theory for estimating the force and moments acting upon spinning airplanes is of interest. For example, strip theory has been used to generate estimates of the aerodynamic characteristics as a function of spin rate for wing-dominated configurations for angles of attack up to 90 degrees. This work, which had been limited to constant chord wings, is extended here to wings comprised of tapered segments. Comparison of the analytical predictions with rotary balance wind tunnel results shows that large discrepancies remain, particularly for those angles-of-attack greater than 40 degrees.

## NOMENCLATURE

b	wing span
c	wing chord
c <sub>o</sub>	wing segment chord at the in-board edge
C <sub>L</sub>	lift coefficient
C <sub>ℓ</sub>	rolling moment coefficient = $\frac{L}{qb \text{ area of segment}}$
C <sub>N</sub>	normal force coefficient
C <sub>N<sub>o</sub></sub>	constant term in normal force coefficient equation
C <sub>N sin α</sub>	coefficient in normal force coefficient equation
h	slope of linear taper equation
L	rolling moment
p	roll rate, $\Omega \cos \alpha$
q	dynamic pressure
q <sub>ℓ</sub>	local dynamic pressure
r	yaw rate, $\Omega \sin \alpha$
V	velocity
V <sub>ℓ</sub>	local velocity
u,v,w	velocity components, center of wing
x,y,z	coordinates
α	angle of attack
α <sub>ℓ</sub>	local angle of attack
ρ	air density
Ω	rotation rate

## INTRODUCTION

The use of parameter estimation in modeling aircraft dynamics has been quite successful for many mathematical models of flight. Parameter estimation is most readily applied when linear models representing small perturbations from straight equilibrium paths are appropriate. Flight data is most accurate in this regime and the mathematical model is the simplest.<sup>1</sup>

Parameter estimation becomes more complex in application to spinning aircraft. Modeling nonlinear aerodynamics, including rotational flow effects, is much more difficult and many more unknown parameters are introduced.<sup>2</sup> In order to reduce the large number of unknowns it is helpful to apply strip theory of reference 3. Strip theory "links the wing airfoil section characteristics to the rolling and yawing moment of the wing in spinning flight."<sup>1</sup>

In reference 1, strip theory provided a mathematical model that was used to determine the rolling moment of a wing in spinning flight. Calculated rolling moment forces due to the wing were about 50 percent larger than the experimental rotary balance spin-tunnel measurements of a wing-dominated aircraft. It is the purpose of this paper to expand the existing mathematical model of a spinning wing in order to more closely represent an aircraft in spinning flight, and to further explore the limitations and possibilities of the more general model. Specifically, the strip theory technique of reference 1 will be extended to wings comprised of tapered segments. The same limitation of reference 1 will be used in that the flow angle at each strip location is independent of the incremental lift at other locations.

## DISCUSSION

In order to decrease the complexity of estimating the rolling moment due to spinning, the authors in reference 1 restricted their analysis to the rolling moment produced by an untapered wing of a wing-dominated aircraft. In this paper the approach is extended to wings of arbitrary planform by considering a wing to be made up of sections of differing taper.

Let us first consider the local flow characteristics for the general spanwise location  $y$ , shown in figure 1.

$$V_\ell^2 = (u - ry)^2 + (w + py)^2$$
$$\alpha_\ell = \arctan\left(\frac{w + py}{u - ry}\right) = \arcsin\left(\frac{w + py}{\sqrt{(u - ry)^2 + (w + py)^2}}\right)$$

and

$$q_\ell = \frac{\rho}{2} \left[ (u - ry)^2 + (w + py)^2 \right]$$

For wings having a constant taper, the wing chord can be represented by a linear equation:

$$c = c_o - hy \quad \text{for} \quad y > 0$$

$$c = c_o + hy \quad \text{for} \quad y < 0$$

The equation for rolling moment for a single strip would be:

$$dL = -\frac{\rho}{2} \left[ (u - ry)^2 + (w + py)^2 \right] C_N \left( c_o \pm hy \right) dy$$

For the entire wing the rolling moment becomes:

$$L = -\frac{\rho}{2} \int_{-\frac{b}{2}}^{\frac{b}{2}} \left[ (u - ry)^2 + (w + py)^2 \right] C_N(y) \left( c_o \pm hy \right) y dy$$

In order to easily represent aerodynamic data at high angles of attacks, the normal force coefficient (fig. 2) is given the form:

$$C_N(\alpha) = C_{N_o} + C_{N_{sina}} \sin \alpha$$

It follows then that a single wing section over which the normal force equation is applicable will have the following contribution to rolling moment:

$$\Delta L = -\frac{\rho c_o C_{N_o}}{2} \int_{y_{lower}}^{y_{upper}} \left[ (u - ry)^2 + (w + py)^2 \right] y dy +$$

$$\frac{hp C_{N_o}}{2} \int_{y_{lower}}^{y_{upper}} \left[ (u - ry)^2 + (w + py)^2 \right] y^2 dy -$$

$$\frac{\rho c_o C_{N_{sina}}}{2} \int_{y_{lower}}^{y_{upper}} \sqrt{(u - ry)^2 + (w + py)^2} (w + py) y dy +$$

$$\frac{hp C_{N_{sina}}}{2} \int_{y_{lower}}^{y_{upper}} \sqrt{(u - ry)^2 + (w + py)^2} (w + py) y^2 dy$$

After integrating,

$$\begin{aligned} \Delta L = & -\frac{\rho c_o C_{N_o}}{2} \left[ \frac{1}{4} A \left( y_{upper}^4 - y_{lower}^4 \right) + \frac{1}{3} B \left( y_{upper}^3 - y_{lower}^3 \right) \right. \\ & \left. + \frac{1}{2} C \left( y_{upper}^2 - y_{lower}^2 \right) \right] + \frac{hp C_{N_o}}{2} \left[ \frac{1}{5} A \left( y_{upper}^5 - y_{lower}^5 \right) \right. \end{aligned}$$

$$\begin{aligned}
& + \frac{1}{4} B \left( y_{\text{upper}}^4 - y_{\text{lower}}^4 \right) + \frac{1}{3} C \left( y_{\text{upper}}^3 - y_{\text{lower}}^3 \right) \Big] \\
& - \frac{w p_c C_N \sin \alpha}{2} \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} y dy - \frac{\rho C_N \sin \alpha}{2} \left( p c_o \pm w h \right) \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} y^2 dy \\
& \mp \frac{p p h C_N \sin \alpha}{2} \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} y^3 dy
\end{aligned}$$

where:

$$A = p^2 + r^2 = \Omega^2$$

$$B = -2ur + 2wp = 0$$

$$C = u^2 + w^2 = V^2$$

$$\Phi = Ay^2 + By + C$$

$$\begin{aligned}
\int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} dy &= \frac{1}{4A} \left[ \left( 2Ay_{\text{upper}} \right) + B \sqrt{Ay_{\text{upper}}^2 + By_{\text{upper}} + C} \right. \\
&\quad \left. - \left( 2Ay_{\text{lower}} \right) + B \sqrt{Ay_{\text{lower}}^2 + By_{\text{lower}} + C} \right] \\
&\quad + \frac{4AC - B^2}{8A \sqrt{A}} \log \left[ \frac{2Ay_{\text{upper}} + B + 2 \sqrt{A^2 y_{\text{upper}}^2 + ABy_{\text{upper}} + AC}}{\sqrt{2Ay_{\text{lower}} + B + 2 \sqrt{A^2 y_{\text{lower}}^2 + ABy_{\text{lower}} + AC}}} \right]
\end{aligned}$$

$$\begin{aligned}
\int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} y dy &= \frac{1}{3A} \left[ \left( Ay_{\text{upper}}^2 + By_{\text{upper}} + C \right)^{3/2} \right. \\
&\quad \left. - \left( Ay_{\text{lower}}^2 + By_{\text{lower}} + C \right)^{3/2} \right]
\end{aligned}$$

$$\begin{aligned}
& - \frac{B}{2A} \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} \, dy \\
& \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} \, y^2 \, dy = \frac{6Ay_{\text{upper}} - 5B}{24A^2} \left( Ay_{\text{upper}}^2 + By_{\text{upper}} + C \right)^{3/2} \\
& \quad - \frac{6Ay_{\text{lower}} - 5B}{24A^2} \left( Ay_{\text{lower}}^2 + By_{\text{lower}} + C \right)^{3/2} \\
& \quad - \frac{4AC - 5B^2}{16A^2} \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} \, dy \\
& \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} \, y^3 \, dy = \left( \frac{y_{\text{upper}}^2}{5A} - \frac{7By_{\text{upper}}}{40A^2} + \frac{7B^2}{48A^3} - \frac{2C}{15A^2} \right) \left( Ay_{\text{upper}}^2 + By_{\text{upper}} + C \right)^{3/2} \\
& \quad - \left( \frac{y_{\text{lower}}^2}{5A} - \frac{7By_{\text{lower}}}{40A^2} + \frac{7B^2}{48A^3} - \frac{2C}{15A^2} \right) \left( Ay_{\text{lower}}^2 + By_{\text{lower}} + C \right)^{3/2} \\
& \quad - \left( \frac{7B^3}{32A^3} - \frac{3CB}{8A^2} \right) \left( \int_{y_{\text{lower}}}^{y_{\text{upper}}} \sqrt{\Phi} \, dy \right)
\end{aligned}$$

The terms in the normal force equation,  $C_{N_o}$  and  $C_{N_{\sin\alpha}}$ , correspond to the local angle-of-attack ranges (see fig. 2) listed in Table 1 from reference 1:

Angle-of-Attack	$C_{N_o}$	$C_{N_{\sin\alpha}}$
-164° to -16°	-0.5	1.0
-16° to -10.5°	-1.6	-3.0
-10.5° to 10.5°	0	5.8
10.5° to 16°	1.6	-3.0
16° to 164°	0.5	1.0

Table 1

The wing span locations having local angles of attack of -16, -10.5, 10.5 and 16 degrees are determined by:

$$y_{\text{boundary}} = \frac{w - u \tan(\alpha_{\text{boundary}})}{-p - r \tan(\alpha_{\text{boundary}})}$$

These will serve as limits of integration in the above equations if they fall in the confines of the panel being considered. If they do not, the boundaries of the panel will be used as limits.

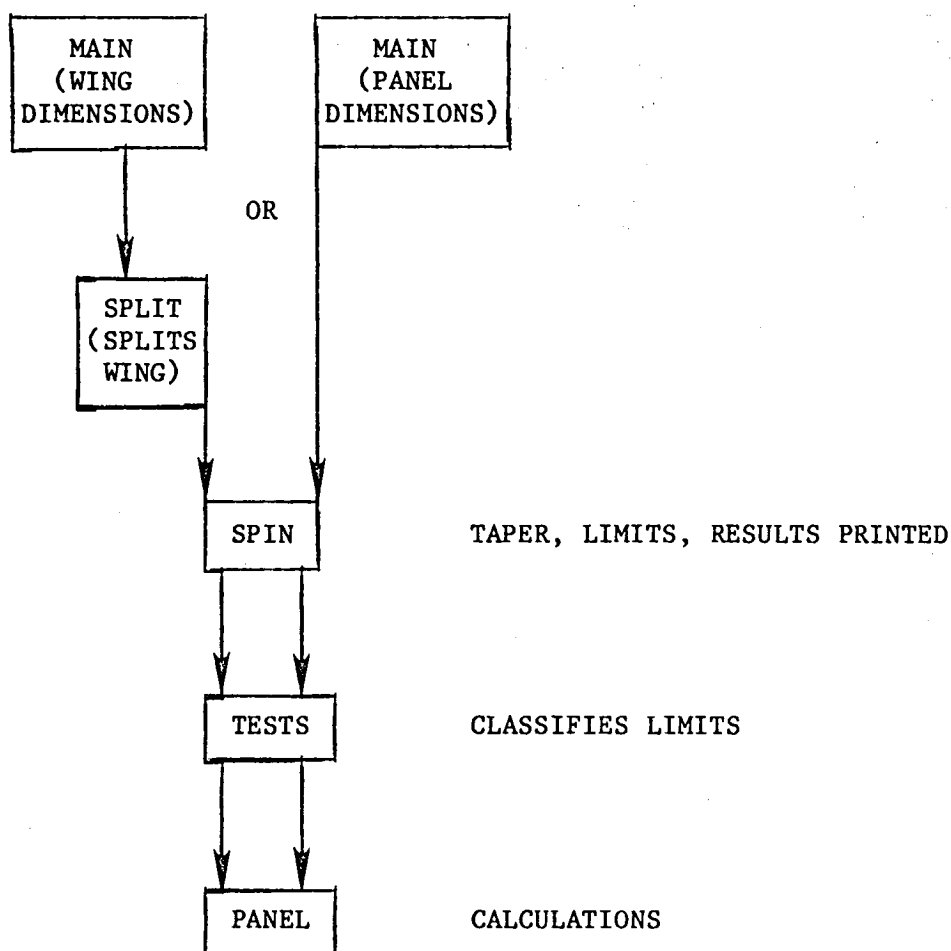
The program used to calculate the rolling moment of the wing using the above equations is listed in the appendix. It is a series of subroutines that will calculate the rolling moment coefficient of any tapered section of a flat wing given the following data: the two boundary chord lengths of each panel; the distance of these chords from the origin; the air density; the velocity of the aircraft; the wingspan; and the area of the wing. There is an option to calculate the rolling moment coefficient of a single panel, or both symmetrical panels having the given dimensions.

The spin subroutine accepts the dimensions of the panel and calculates the slope of the linear equation describing wing taper (h). It then computes the limits of integration along the panel. These limits are sent to the intermediate tests subroutine. Tests classifies the limits and sends only those that are within the bounds of the desired panel(s) to the panel subroutine. The panel subroutine does the actual rolling moment calculation of the panel between the limits using the above equations. The split subroutine is an optional subroutine which, given the dimensions of the wing, will split a wing into its component panels and send each panel in succession to the spin subroutine.

With this program, a wing comprised of tapered panels can be modeled, panel by panel. Through a simple modification, the program can accumulate the total rolling moment of an aircraft wing due to each panel at a selected angle-of-attack. For the airplane shown in figure 3, this was done at an angle-of-attack of 14 degrees in order to obtain figure 4. Figure 4 is a plot of the total rolling moment coefficient of the wing of the aircraft, as well as the rolling moment coefficient of each of the wing's component panels as a function of nondimensional spin rate. The bottom curve of figure 4 represents the total rolling moment coefficient for the airplane of figure 3 at 14 degrees angle-of-attack.



The following flowchart is a diagram of the program:



In a typical light, wing-dominated aircraft such as the one illustrated in figure 3, the panels that cause the greatest moment are the outer panels as is shown in figure 4 and in table 2. The upper curve in figure 4 represents the rolling moment contribution of the inner panels, the next curve represents the contribution of the middle panels and the third curve from the top is the contribution of the outer panels. This figure is for a fixed angle-of-attack while the rotation rate varies. On the other hand, table 1 shows the relationship between the panels when the rotation rate is fixed and the angle-of-attack is varied. The data of table 1 and Figure 4 clearly show that the outer panels contribute from 78% to 97% of the total rolling moment. Of course, this is expected since these panels are larger than the others, have the longest moment arm, and experience the greatest variation in dynamic pressure.

Figure 5 shows the improvement caused by taking into account wing taper as compared to the values obtained with a constant chord. There is significant improvement in the data, particularly at higher rates of rotation. The upper curves are the spin-tunnel test data. Obviously, improvements in the model must be made before the method can be considered acceptable. It is interesting to note (see figures 5 and 6) that there is little difference when the wing of the aircraft in figure 3 is simplified in the calculations to two large trapezoidal panels instead of six smaller ones. However, the multi-panel approach is more accurate and is applicable to the more general case.

In reference 1, it was noted that at angles-of-attack around 50 degrees the experimental rolling moments were autorotative at low rotation rates. The calculated data of reference 1 did not represent this phenomenon. The plot of 30 and 50 degrees angle-of-attack in figure 7 shows that the new calculated data does not show autorotative moments either. With the theory being used here, it would be impossible to obtain autorotative moments except over an angle-of-attack range of 10.5 to 16 degrees since the slope of the line of normal force coefficient vs. angle-of-attack (fig. 2) is always positive except over this range. Note that figures 5 and 6 show an autorotative moment at low rates of rotation both in the test data and in the calculated data for 14 degrees angle-of-attack. However, an extension must be made to this simplified aerodynamic theory for higher angles-of-attack.<sup>1</sup>

The amount of error in the mathematical representation of a spinning wing has been decreased by describing the wing as a set of tapered panels. However, the errors are still large. The next step might be to consider the contribution of the tail section to the rolling moment. Since the program calculates the rolling moment of any tapered panel, the three tail panels could be input in order to determine the tail effects. The present method will compute the rolling moment for swept-wing configurations since rolling moment is independent of sweep. However, an extension of the model should also incorporate pitching moment. Of course, this method will not hold for aircraft where body effects cannot be neglected. The effects of the body would have to be considered by some other method such as the strip theory of reference 5. Improved estimates of aerodynamic moments would be expected if the induced flow effects on the flow angles were included in the formulation. Past results and future extensions promise further improvements in predicting the aerodynamic forces and moments of spinning airplanes.

#### CONCLUDING REMARKS

Mathematical representations of nonlinear phenomena such as the aerodynamics of a spinning aircraft are characterized by having large numbers of unknown parameters. Analytical methods such as strip theory can be used to reduce the number of unknown parameters. In this paper, strip theory is applied to compute aerodynamic forces for a wing composed of several variable taper trapezoidal panels in order to obtain a model structure which requires only the unknowns of the normal force equations. Although the error is decreased significantly by using strip theory in this manner as compared to approximating the wing as untapered, there is still much more to be done in order to analytically predict aerodynamic force of spinning aircraft. In order to extend the model further, many new parameters would have to be added. Also, it is clear that aerodynamic theory for angles-of-attack greater than 40 degrees must be improved since it is impossible to predict the results of spin-tunnel rotary balance tests with strip theory methods.

Since the program that calculates the data is general enough to accept any wing panel of an aircraft, the revised model is currently useful in comparing the effects on a panel of changing parameters such as rotation rate, angle-of-attack, velocity, taper, etc. It is also useful for comparing aircraft components. However, the error between analytical predictions and the experimental data is still too large to consider the strip theory representation to be an effective model of a spinning aircraft.

## APPENDIX

Listed in the following pages is the program used to calculate the rolling moment due to spin rate for an arbitrary planform wing. Inputs to the program are set in a short main program which calls the subroutines necessary for the calculations.

The first page shows an example of the simplest case where a single panel is input to the program. Variable CHORD is the inboard chord length and CHTIP is the outboard chord length. D1 and D2 are spanwise distances from the center line of the fuselage to CHORD and CHTIP respectively. AREA refers to the area of the entire wing containing the panel, and SPAN is the wing span. RHO is air density and VEL is the velocity of the aircraft. The last integer tells the program whether to compute the rolling moment for panel with the given dimensions on the positive side of the aircraft (0), the negative side of the aircraft (1) or both (2). Normally, this value will be 2, except when isolation a single wing panel is desired.

The second page shows a case where the panels of an entire wing will be input to the program. In this case, variable CHORD is the root chord, CH1 and CH2 are the chord lengths at the point of wing taper change, and CHTIP is the chord length at the wing tip. D1 and D2 are the spanwise distances from the center line to CH1 and CH2 respectively. FUSE is the width of the fuselage.

As was mentioned in the text, the program can be modified to accumulate the total rolling moment of a multi-paneled wing. To do this, a one-dimensional array can be defined and placed inside the main loop of the spin subroutine such that each time spin is called with a new panel's dimensions, the nine values of the panel's rolling moment coefficient array (CLW) are added to the new array for a selected angle-of-attack (corresponding to an iteration of the main loop). For more than one angle-of-attack, a two-dimensional array would be necessary.

PROGRAM MAIN 76/76 OPT=1 FTH 4.8+992 04/03/02. 00.5

```

1      PROGRAM MAIN(INPUT,OUTPUT)
      CHORD=3.41
      CHTIP=1.01
      CM1=2.97
      CM2=2.97
      D1=1.045
      D2=10.0
      SPAN=20.
      FUSE=2.09
      RMD=.002370
10     VEL=100.
      AREA=52.2
      CALL SPIN(CHORD,CHTIP,D1,D2,AREA,SPAN,RMD,VEL,2)
      STOP
15     END

```

# SYMBOLIC REFERENCE MAP (R=1)

ENTRY POINTS  
4140 MAIN

VARIABLES	SM	TYPE	RELOCATION		
4223 AREA	REAL			4211 CHORD	REAL
4212 CHTIP	REAL			4213 CM1	REAL
4214 CM2	REAL			4215 D1	REAL
4216 D2	REAL			4220 FUSE	REAL
4221 RMD	REAL			4217 SPAN	REAL
4222 VEL	REAL				

FILE NAMES      MODE  
0 INPUT      2054 OUTPUT

EXTERNALS      TYPE      ARGS  
SPIN      9

STATISTICS  
PROGRAM LENGTH      2158      141  
BUFFER LENGTH      40078      2055

PROGRAM MAIN 76/76 OPT=1 FTH 4.8+992 04/03/03. 00.6

```

1      PROGRAM MAIN(INPUT,OUTPUT)
      CHORD=3.41
      CHTIP=1.099
      CM1=2.97
      CM2=2.97
      D1=2.22
      D2=4.06
      SPAN=20.
      FUSE=2.09
      RMD=.002370
10     VEL=100.
      AREA=55.04
      CALL SPLIT(CHORD,CM1,CM2,CHTIP,D1,D2,SPAN,FUSE,RMD,AREA,VEL)
      STOP
15     END

```

# SYMBOLIC REFERENCE MAP (R=1)

ENTRY POINTS  
4140 MAIN

VARIABLES	SM	TYPE	RELOCATION		
4224 AREA	REAL			4212 CHORD	REAL
4213 CHTIP	REAL			4214 CM1	REAL
4215 CM2	REAL			4216 D1	REAL
4217 D2	REAL			4220 FUSE	REAL
4222 RMD	REAL			4220 SPAN	REAL
4223 VEL	REAL				

FILE NAMES      MODE  
0 INPUT      2054 OUTPUT

EXTERNALS      TYPE      ARGS  
SPLIT      11

STATISTICS  
PROGRAM LENGTH      2168      142  
BUFFER LENGTH      40078      2055

```

1      C      SUBROUTINE SPINICH1,CH2,D1,D2,AREA,SPANV,RHO1,VEL,ITOG)
      C
      C      *****
      C      * THIS SUBROUTINE GENERATES NON-DIMENSIONALIZED VALUES FOR THE *
      C      * ROLLING MOMENT OF A SPINNING AIRCRAFT WING PANEL AT ANGLES OF *
      C      * ATTACK FROM 0 TO 90 DEGREES AND AT NON-DIMENSIONALIZED ROTATION *
      C      * RATES FROM 0 TO .9. THE MAIN PROGRAM MUST DEFINE VALUES FOR THE *
      C      * BOUNDARY CHORDS, THE DISTANCES TO THESE CHORDS FROM THE ORIGIN, *
      C      * THE WINGSPAN, THE VELOCITY OF THE AIRCRAFT, THE AIR DENSITY, THE *
      C      * AREA OF THE WING, AND AN INTEGER TO SPECIFY WHETHER OR NOT THE *
      C      * USER WANTS TO DESCRIBE A NEGATIVE PANEL, POSITIVE PANEL OR BOTH. *
      C      * THE PRIMARY PURPOSE OF THIS SUBROUTINE IS TO COMPUTE THE LIMITS *
      C      * OF INTEGRATION ON THE PANEL. *
      C      *****
13     C
      C      DEFINITION OF VARIABLES
      C
      C      ALPHA - THE ANGLE OF ATTACK IN RADIAN
      C      ALPHD - THE ANGLE OF ATTACK IN DEGREES
20     C      A1 - THE FIRST LOCATIONAL ANGLE OF ATTACK - 10.5 DEGREES
      C      A2 - THE SECOND LOCATIONAL ANGLE OF ATTACK - 16 DEGREES
      C
      C      CH1, CH2 - TWO LIMIT CHORDS OF THE PANEL
      C      (CH2 IS LARGER THAN CH1)
25     C
      C      CLV - NON-DIMENSIONALIZED ARRAY FOR ROLLING MOMENT
      C      CNSA - CONSTANT TERM IN NORMAL FORCE COEFFICIENT EQUATION
      C      CNO - COEFFICIENT IN NORMAL FORCE COEFFICIENT EQUATION
30     C
      C      D1 - DISTANCE TO CH1
      C      D2 - DISTANCE TO CH2
      C
      C      ELW - ROLLING MOMENT
35     C
      C      M - SLOPE OF THE LINEAR EQUATION DESCRIBING THE WING TAPER
      C      ITOG = 0 FOR POSITIVE PANEL; 1 FOR NEGATIVE PANEL; 2 FOR BOTH
      C
      C      LA, LB, LC, LD, LE - LOWER LIMITS OF INTEGRATION
      C      UA, UB, UC, UD, UE - UPPER LIMITS OF INTEGRATION
40     C
      C      OMEGA - ROTATION RATE

```

```

      C      P - ROLL RATE
      C      QUE - DYNAMIC PRESSURE
45     C      R - TAN RATE
      C      RHO - AIR DENSITY
      C
      C      SPAN - WING SPAN
      C
      C      U - COMPONENT OF VELOCITY
      C      VEL - VELOCITY
      C      W - COMPONENT OF VELOCITY
      C      WBSV - NON-DIMENSIONALIZED ROTATION RATE
50     C
      C      YH1 - SPAN LOCATION HAVING AN ANGLE OF ATTACK OF -10.5 DEGREES
      C      YH2 - SPAN LOCATION HAVING AN ANGLE OF ATTACK OF -16 DEGREES
      C      Y1 - SPAN LOCATION HAVING AN ANGLE OF ATTACK OF 10.5 DEGREES
      C      Y2 - SPAN LOCATION HAVING AN ANGLE OF ATTACK OF 16 DEGREES
55     C
      C
      C      DIMENSION CLV(50)
      C      FORMAT(11E12.4)
      C      REAL LA, LB, LC, LD, LE, MFUSE
      C      COMMON // A,B,C,M,P,M, MFUSE, SPAN, CNO, CNSA, ELW, CHORD, RHO
60     C
      C
      C      A1=10.5/57.3
      C      A2=16./57.3
      C      RHO=RHO1
      C      SPAN=SPANV
      C      MFUSE=01
      C      M=(CH1-CH2)/(D2-D1)
      C      CHORD=CH1+M*(A2-D1)
      C      QUE=.3*RHO*VEL*VEL
      C      ALPHA=-2./57.3
70     C
      C      BEGINNING FIRST LOOP
      C
      C      DO 1 I=1,46
80     C
      C      INCREMENTING ANGLE OF ATTACK BY 2 DEGREES
      C
      C      ALPHA=ALPHA+2./57.3
      C      ALPHD=97.3*ALPHA

```

```

SUBROUTINE SPIN      74/74  OPT=1      FTH 4.0+552      04/03/05. 09.00
85      W=VEL*SIN(ALPHA)
      U=VEL*COS(ALPHA)
      W2V=0.
      C
      C BEGINNING SECOND LOOP
      C
90      DO 2 J=1,9
      C
      C INCREMENTING ROTATION RATE
      C
95      W2V=W2V+.1
      OMEGA=W2V*.2*.0VEL/SPAN
      P=OMEGA*COS(ALPHA)
      R=OMEGA*SIN(ALPHA)
      A=P*P+R*R+.000000001
      B=-2.0U*W+.2*W*P
      C=U*U+W*W
      YR2=(-W*U*TAN(A2))/(P+R*TAN(A2))
      YR1=(-W*U*TAN(A1))/(P+R*TAN(A1))
      Y1=(-W*U*TAN(A1))/(P+R*TAN(A1))
      Y2=(-W*U*TAN(A2))/(P+R*TAN(A2))
100      LA=777.
      LB=777.
      LC=777.
      LD=777.
      LE=777.
110      UA=777.
      UB=777.
      UC=777.
      UD=777.
      UE=777.
115      ELW=0.
      C
      C COMPUTING THE LIMITS UA & LA FOR CNO=-.5 AND CNSA=1.0
      C
120      IF(-D2-YR2)11,11,100
      11 LA=-D2
      IF(D2-YR2)12,12,13
      13 UA=YR2
      GO TO 10
125      12 UA=D2
      10 CONTINUE

```

```

SUBROUTINE SPIN      74/74  OPT=1      FTH 4.0+552      04/03/05. 09.00
      CNO=-.5
      CNSA=1.0
      CALL TESTS(UA,LA,ITOG)
130      100 CONTINUE
      C
      C COMPUTING THE LIMITS UB & LB FOR CNO=-1.0 AND CNSA=-3.
      C
135      IF(-D2-YR1)14,14,130
      14 IF(D2-YR2)150,150,16
      16 IF(-D2-YR2)17,17,18
      18 LB=-D2
      GO TO 19
      17 LB=YR2
140      19 IF(D2-YR1)21,21,20
      21 UB=D2
      GO TO 15
      20 UB=YR1
145      15 CONTINUE
      CNO=-1.0
      CNSA=-3.
      CALL TESTS(UB,LB,ITOG)
150      130 CONTINUE
      C
      C COMPUTING THE LIMITS UC & LC FOR CNO=0.0 AND CNSA=5.0
      C
155      IF(-D2-Y1)22,22,230
      22 IF(D2-YR1)230,230,24
      24 IF(-D2-YR1)25,25,26
      26 LC=-D2
      GO TO 27
      25 LC=YR1
160      27 IF(D2-Y1)28,28,29
      28 UC=D2
      GO TO 23
      29 UC=Y1
      23 CONTINUE
      CNO=0.
      CNSA=5.0
      CALL TESTS(UC,LC,ITOG)
165      230 CONTINUE
      C
      C COMPUTING THE LIMITS UD & LD FOR CNO=1.0 AND CNSA=-3.

```

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170      C
      IF(D2-V2)30,30,310
30      IF(D2-V1)310,310,32
32      IF(D2-V1)33,33,34
34      LD=D2
      GO TO 35
175      35 LD=Y1
      35 IF(D2-V2)36,36,37
36      UD=D2
      GO TO 31
37      UD=Y2
31      CONTINUE
      CNO=1.0
      CNSA=3.
      CALL TESTS(UD,LD,ITOG)
180      310 CONTINUE
185      C
      C COMPUTING THE LIMITS UE & LE FOR CNO=.9 AND CNSA=1.0
      C
      IF(D2-V2)380,380,39
39      IF(D2-V2)40,40,41
190      41 LE=D2
      GO TO 42
      40 LE=Y2
      42 UE=D2
      CNO=.9
      CNSA=1.0
195      CALL TESTS(UE,LE,ITOG)
      380 CONTINUE
      C
      C PRINTING THE LIMITS TO THE DUMP
      C
200      PRINT 700,LA,UA,LB,UB,LC,UC,LD,UD,LE,UE
      C
      C COMPUTING THE NON-DIMENSIONALIZED ROLLING MOMENT FROM THE ROLLING MOMENT.
      C THIS WILL HAPPEN 9 TIMES AND THEN THE SUBROUTINE WILL EXIT INTO THE OUTER
      C LOOP WHERE THE ANGLE OF ATTACK IS INCREASED BY 2 DEGREES.
205      C
      CLW(J)=ELW/IQUE*AREA*SPAN
      2 CONTINUE
      C
210      C PRINTING THE ANGLE OF ATTACK AND THE NON-DIMENSIONALIZED ROLLING MOMENT

```

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      C
      PRINT 700,ALPHD,(CLW(J),J=1,9)
      1 CONTINUE
      C
215      C THE SUBROUTINE WILL END AT ANGLE OF ATTACK EQUAL TO 90 DEGREES
      C
      RETURN
      END

```

# SYMBOLIC REFERENCE MAP (R-1)

## ENTRY POINTS 3 SPIN

VARIABLES	SN	TYPE	RELOCATION			
0 A		REAL	/ /	407 ALPHA	REAL	
411 ALPHD		REAL	/ /	0 AREA	REAL	F.P.
404 A1		REAL	/ /	409 A2	REAL	
1 B		REAL	/ /	2 C	REAL	/ /
13 CMORD		REAL	/ /	0 CM1	REAL	F.P.
0 CM2		REAL	F.P.	430 CLW	REAL	ARRAY
11 CNSA		REAL	/ /	10 CNO	REAL	/ /
0 DI		REAL	F.P.	0 DZ	REAL	F.P.
12 ELW		REAL	/ /	5 H	REAL	/ /
0 HPUSE		REAL	/ /	410 I	INTEGER	
0 ITOG		INTEGER	F.P.	414 J	INTEGER	
377 LA		REAL	/ /	400 LB	REAL	
401 LC		REAL	/ /	402 LD	REAL	
403 LE		REAL	/ /	415 OMEGA	REAL	
4 P		REAL	/ /	406 QUE	REAL	
416 R		REAL	/ /	14 RMD	REAL	/ /
0 RHOS		REAL	F.P.	7 SPAN	REAL	/ /
0 SPANV		REAL	F.P.	412 U	REAL	
423 UA		REAL	/ /	424 UB	REAL	
425 UC		REAL	/ /	426 UD	REAL	
427 UE		REAL	/ /	0 VEL	REAL	F.P.
3 V		REAL	/ /	413 V82V	REAL	
420 VM1		REAL	/ /	417 VM2	REAL	

```

1      C *****
      C * THIS SUBROUTINE CLASSIFIES LIMITS SENT FROM THE SUBROUTINE SPIN *
      C * INTO THREE CATEGORIES: *
      C * 1) LIMITS THAT BOTH FALL ON THE NEGATIVE WING *
      C * 2) LIMITS THAT BOTH FALL ON THE POSITIVE WING *
      C * 3) LIMITS THAT FALL ON EITHER SIDE OF THE FUSELAGE *
      C * THESE LIMITS ARE SENT TO SUBROUTINE PANEL TO COMPUTE THE *
      C * ROLLING MOMENT. *
      C *****
10     C
      C SUBROUTINE TESTS(UA,LA,ITOG)
      C REAL LA
      C COMMON // A,B,C,W,P,H,MFUSE,SPAN,CNO,CNSA,ELW,CHORD,RHO
19     C ROUTINE TO CATCH LIMITS THAT ARE LESS THAN THE DISTANCE TO THE PANEL.
      C
      C IF(UA.LE.MFUSE.AND.UA.GE.(-MFUSE)) UA=-MFUSE
      C IF(LA.LE.MFUSE.AND.LA.GE.(-MFUSE)) LA=-MFUSE
      C IF(UA.LE.LA) GO TO 1101
20     C
      C IF DOUBLE PANEL NOT REQUESTED, GO TO 1190
      C
      C IF(ITOG.LE.1) GO TO 1190
29     C
      C >>> DOUBLE PANEL <<<
      C
      C BOTH LIMITS POSITIVE
      C
      C IF(UA.GE.MFUSE.AND.LA.GE.MFUSE) GO TO 1100
30     C
      C BOTH LIMITS NEGATIVE
      C
      C IF(UA.LE.-MFUSE.AND.LA.LE.-MFUSE) GO TO 1100
39     C
      C LIMITS THAT COME THROUGH ARE THOSE THAT ARE NOT ON THE SAME PANEL.
      C THEREFORE, THE ROLL MOMENT MUST BE CALCULATED FOR EACH SIDE SEPARATELY.
      C
      C ***** NEGATIVE WING *****
40     C
      C ORIGA=UA
      C ORIGB=LA
      C UA=-MFUSE

```

```

      C IF(UA.EQ.LA) GO TO 1007
      C CALL PANEL(UA,LA)
49     C
      C ***** POSITIVE WING *****
      C
      C 1007 UA=ORIGA
      C LA=MFUSE
      C IF(UA.EQ.LA) GO TO 1101
      C CALL PANEL(UA,LA)
      C LA=ORIGB
      C GO TO 1101
59     C
      C >>> SINGLE PANEL <<<
      C
      C 1190 ORIGA=UA
      C ORIGB=LA
      C IF(ITOG.GT.0) GO TO 1199
      C IF(UA.GE.MFUSE.AND.LA.GE.MFUSE) GO TO 1100
      C IF(UA.LE.-MFUSE.AND.LA.LE.-MFUSE) GO TO 1101
      C LA=MFUSE
      C IF(UA.LE.LA) GO TO 1101
      C CALL PANEL(UA,LA)
      C LA=ORIGB
      C GO TO 1101
      C 1199 IF(UA.GE.MFUSE.AND.LA.GE.MFUSE) GO TO 1101
      C IF(UA.LE.-MFUSE.AND.LA.LE.-MFUSE) GO TO 1100
      C UA=-MFUSE
      C IF(UA.LE.LA) GO TO 1101
      C CALL PANEL(UA,LA)
      C UA=ORIGA
      C GO TO 1101
      C 1100 CALL PANEL(UA,LA)
79     C 1101 RETURN
      C END

```

SYMBOLIC REFERENCE MAP (R=1)



SUBROUTINE PANEL 74/74 OPT=1 FTM 4.0552 04/07/12.

```

1 C *****
C * THIS SUBROUTINE PERFORMS THE INTEGRATION FOR THE ROLLING MOMENT *
C * OF THE PANEL. TWO LIMITS ARE SENT HERE FROM SUBROUTINE *
C * TESTS THAT ARE BOTH EITHER ON A POSITIVE PANEL OR A NEGATIVE *
C * PANEL. THE SUBROUTINE IS CALLED EACH TIME A NEW SET OF LIMITS *
C * ON THE PANEL IS COMPUTED. *
C *****
C DEFINITION OF VARIABLES
10 C
C M - THE SLOPE OF THE LINEAR EQUATION DESCRIBING WING TAPER
C
C PHI - INTEGRAL OF THE SQUARE ROOT OF AY**2 + BY + C
C PHIY - Y TIMES THE INTEGRAL OF THE SAME
15 C
C PHIY2 - INTEGRAL OF Y SQUARED TIMES THE SAME
C
C PHIY3 - INTEGRAL OF Y CUBED TIMES THE SAME
C
C RADL - SQUARE ROOT OF AY**2 + BY + C AT THE LOWER LIMIT
C RADU - SQUARE ROOT OF AY**2 + BY + C AT THE UPPER LIMIT
20 C
C SUBROUTINE PANEL(IA,LA)
C REAL LA
C COMMON // A,B,C,M,P,H,MFUSE,SPAN,CNO,CNSA,FLV,CMRD,RMD
C
C RADU=SQRT(A*UA**2+B*UA+C)
C RADL=SQRT(A*LA**2+B*LA+C)
C
C PHI=(UA*.5+.25/A)*RADU-(LA*.5+.25/A)*RADL
C PHI=PHI+(4.*A*C-B*B)/(8.*A*SQRT(A))*((ALOG(A*UA**2+B*UA+C)/
30 C IADU)-ALOG(A*LA**2+B*LA+C)/RADL))
C
C PHIY=.333333*(RADU**3-RADL**3)/A+.5*B*PHI/A
C
C PHIY2=(6.*A*UA -.5.*B)*RADU**3-(6.*A*LA-.5.*B)*RADL**3/(24.*A*B)
C PHIY2=PHIY2-(4.*A*C-B*B)*PHI/(16.*A*B)
35 C
C
C TEMP=(UA**2/(5*A)-(7*B*UA)/(40*A*B)+(7*B*B)/(48*A**3))
C PHIY3=(TEMP-(2*C)/(15*A*A))*RADU**3
C TEMP=(LA**2/(5*A)-(7*B*LA)/(40*A*B)+(7*B*B)/(48*A**3))
C PHIY3=PHIY3-(TEMP-(2*C)/(15*A*A))*RADL**3
40 C PHIY3=PHIY3-(17*B**3)/(32*A**3)-(13*C*B)/(16*A**3)*PHI
C

```

SUBROUTINE PANEL 74/74 OPT=1 FTM 4.0552 04/07/12. 1.

```

C
C LIMITS THAT ARE ON THE POSITIVE SIDE OF THE WING MUST GO THROUGH THE
45 C EQUATIONS AT 2000 INSTEAD OF THOSE FOLLOWING BECAUSE THE NEGATIVE WING
C IS DESCRIBED BY A DIFFERENT EQUATION THAN THE POSITIVE SIDE.
C
C IF(UA*GE*MFUSE.AND.LA*GE*MFUSE) GO TO 2000
C
50 C
C FLV=FLV+P*H*CMRD*.5*CNO*(.25*A*(UA**4-LA**4)+.333333*B*(UA**3-LA
C 1**3)+C*.5*(UA**5-LA**5))
C SHORHT=CNO*.5*(.25*A*(UA**5-LA**5)+.25*B*(UA**4-LA**4)+.333333*C
55 C *(UA**3-LA**3))
C GO TO 2000
C
C 2000 FLV=FLV+P*H*CMRD*.5*CNSA*PHIY
C SHORHT=CNSA*.5*(P*H*CMRD-B*H)*PHIY2+P*H*H*CMNSA*.5*PHIY3
C FLV=FLV+P*H*CMRD*.5*CNO*(.25*A*(UA**4-LA**4)+.333333*B*(UA**3-LA
60 C 1**3)+C*.5*(UA**5-LA**5))
C SHORHT=CNO*.5*(.25*A*(UA**5-LA**5)+.25*B*(UA**4-LA**4)+.333333*C
C *(UA**3-LA**3))
C 2000 RETURN
C END

```

# SYMBOLIC REFERENCE MAP (0=1)

ENTRY POINTS  
3 PANEL

VARIABLES	SM	TYPE	RELOCATION				
0 A	REAL			1 B	REAL		
2 C	REAL			13 CMRD	REAL		
11 CNSA	REAL			10 CNO	REAL		
12 ELV	REAL			5 H	REAL		
6 MFUSE	REAL			0 LA	REAL		F.P.
6 P	REAL			334 PHI	REAL		
335 PHIY	REAL			336 PHIY2	REAL		
346 PHIY3	REAL			333 RADL	REAL		
332 RADU	REAL			14 RMD	REAL		

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```

1 C .....
2 C * THIS SUBROUTINE SPLITS A WING INTO ITS INDIVIDUAL PANELS *
3 C * AND SENDS THE DIMENSIONS TO SUBROUTINE SPIN. THE USER *
4 C * MUST SUPPLY IN THE MAIN PROGRAM VALUES FOR THE COMMON *
5 C * CMORD, THE TIP CMORD, AND TWO CMORDS IN-BETWEEN AT THE *
6 C * POINTS OF TAPER CHANGE, THE DISTANCES TO THESE CMORDS FROM *
7 C * THE ORIGIN, THE AREA OF THE WING, THE WINGSPAN, AIR DEN- *
8 C * SITY, THE VELOCITY OF THE AIRCRAFT AND THE WIDTH OF THE *
9 C * FUSELAGE. *
10 C .....
11 C SUBROUTINE SPLIT(CMORD,CM1,CM2,CHTIP,D1,D2,SPAN,FUSE,RNO,AREA,VEL)
12 C
13 C MFUSE=.5*FUSE
14 C HSPAN=.5*SPAN
15 C CALL SPIN(CMORD,CM1,MFUSE,D1,AREA,SPAN,RNO,VEL,2)
16 C CALL SPIN(CM1,CM2,D1,D2,AREA,SPAN,RNO,VEL,2)
17 C CALL SPIN(CM2,CHTIP,D2,HSPAN,AREA,SPAN,RNO,VEL,2)
18 C RETURN
19 C END
20

```

**SYMBOLIC REFERENCE MAP (R=1)**

ENTRY POINTS  
3 SPLIT

VARIABLES	SN	TYPE	RELOCATION				
0 AREA		REAL	F.P.P.	0	CHORD	REAL	F.P.P.
0 CHTIP		REAL	F.P.P.	0	CHI	REAL	F.P.P.
0 CHZ		REAL	F.P.P.	0	CI	REAL	F.P.P.
0 DZ		REAL	F.P.P.	0	FUSE	REAL	F.P.P.
116 MFUSE		REAL	F.P.P.	117	HSPAN	REAL	F.P.P.
0 RMO		REAL	F.P.P.	0	SPAN	REAL	F.P.P.
0 VEL		REAL	F.P.P.				
EXTERNALS		TYPE	ARGS				
SPIN			9				

## REFERENCES

1. Taylor, Lawrence W., Jr.; and Pamadi, Bandu N.: Estimation of Parameters Involved in High Angle-of-Attack Aerodynamic Theory Using Spin-Flight Test Data. AIAA Atmospheric Flight Mechanics Conference, Gatlinburg, TN, August 1983.
2. Taylor, Lawrence W., Jr.: Applications of Parameter Estimation in the Study of Spinning Airplanes. AIAA 9th Atmospheric Flight Mechanics Conference, San Diego, CA, August 1982.
3. Taylor, Lawrence W., Jr.; Pamadi, Bandu N.: An Evaluation of Aerodynamic Modeling of Spinning Light Airplanes. AIAA 21st Aerospace Sciences Meeting, January 1983.
4. Ralston, John N.: Rotary Balance Data for a Typical Single-Engine General Aviation Design for an Angle-of-Attack Range of 8 to 90. NASA Contractor Report 3246, March 1983.
5. Pamadi, Bandu N.: An Estimation of Aerodynamic Forces and Moments on an Airplane Model Under Steady State Spin Conditions. AIAA 9th Atmospheric Flight Mechanics Conference, San Diego, CA, August 1982.

$\alpha$ , deg.	Inner Panels	Middle Panels	Outer Panels	Total
0	-.00523	-.04370	-.1747	-.2236
2	-.00565	-.04093	-.1759	-.2225
4	-.00564	-.03505	-.1793	-.2200
6	-.00497	-.02923	-.1818	-.2160
8	-.00346	-.02434	-.1830	-.2108
10	-.00180	-.02017	-.1825	-.2045
12	-.000525	-.01620	-.1825	-.1992
14	-.000417	-.01220	-.1796	-.1922
16	-.000768	-.00824	-.1724	-.1814
18	-.000197	-.00451	-.1553	-.1600
20	-.000508	-.00239	-.1378	-.1407
22	-.000882	-.00198	-.1202	-.1231
24	-.001890	-.00394	-.1024	-.1072

Table 2  
Rolling moment coefficient for the contributing trapezoidal panels on the main wing of the airplane shown in figure 3 at angles of attack from 0 to 24 degrees and  $b/2V = 0.5$ .

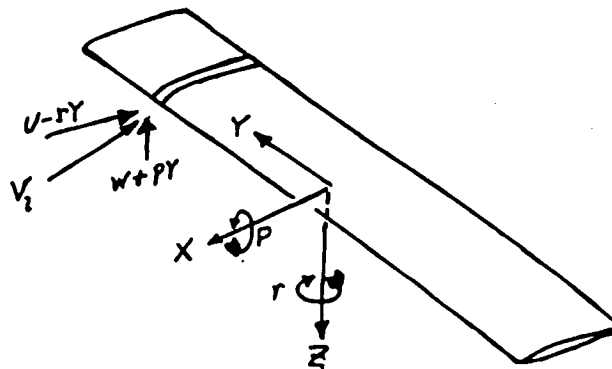


Figure 1. Schematic Sketch of a Spinning Wing

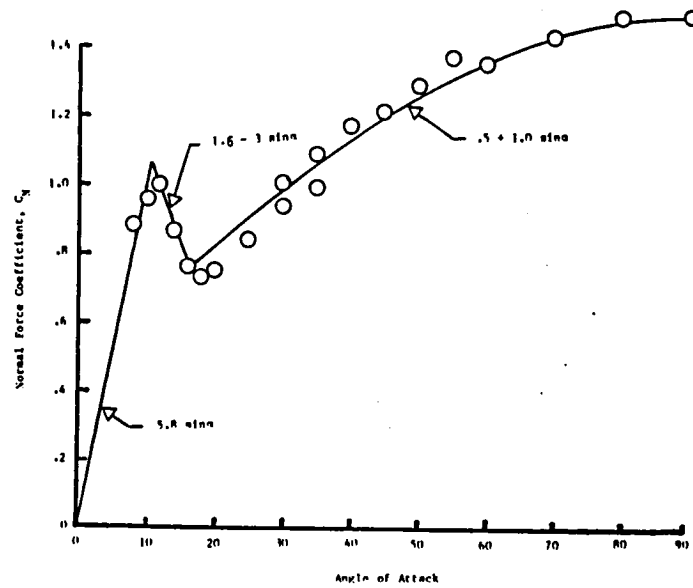


Figure 2. Model and measured normal force coefficient of reference 6.

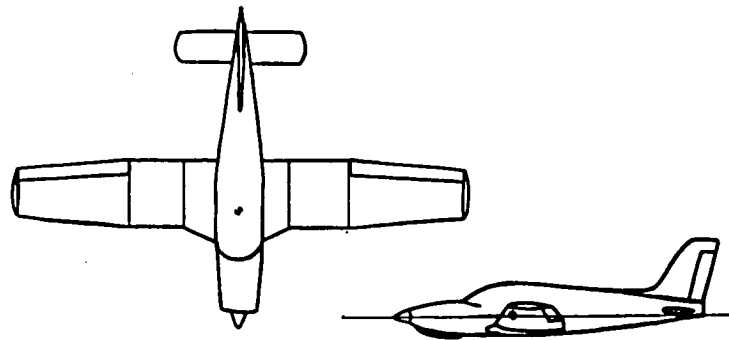


Figure 3. Drawing of 1/16-scale typical light airplane of reference 4. Note the 6 distinct panels on the main wing.

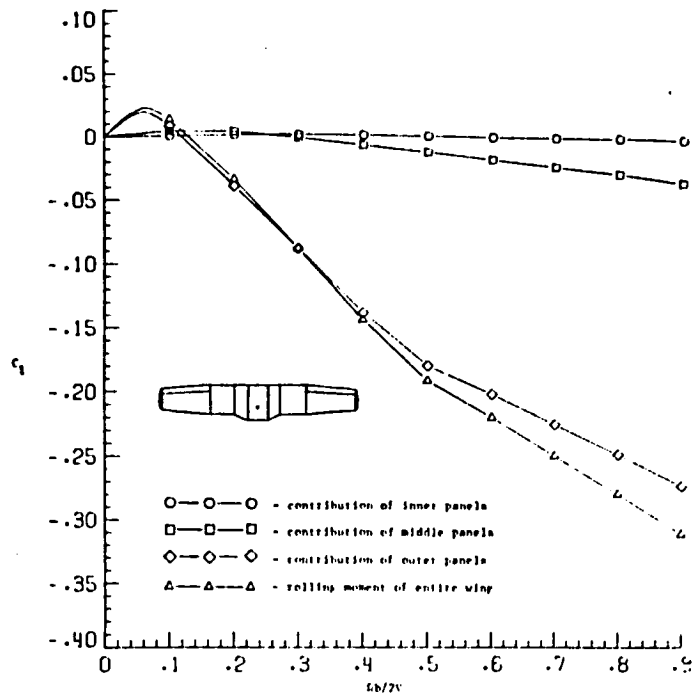


Figure 4. Contribution of wing panels to the rolling moment for 14 degrees angle of attack.

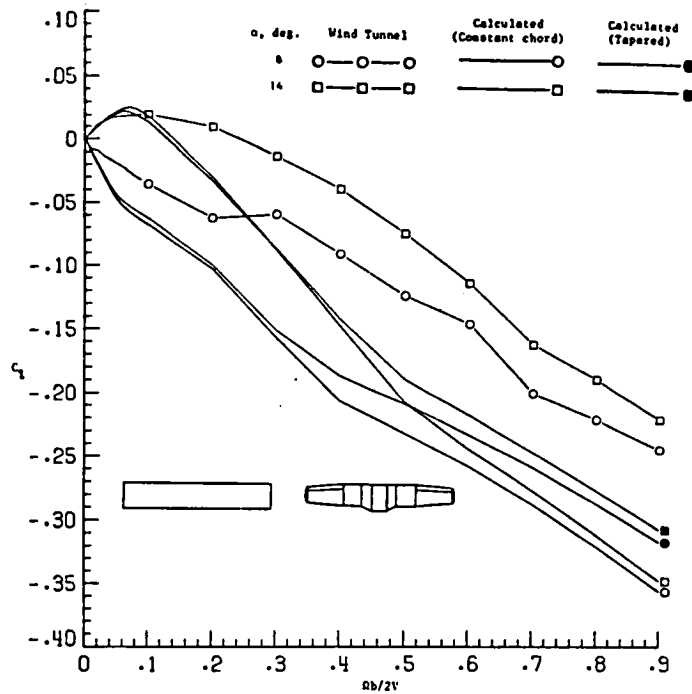
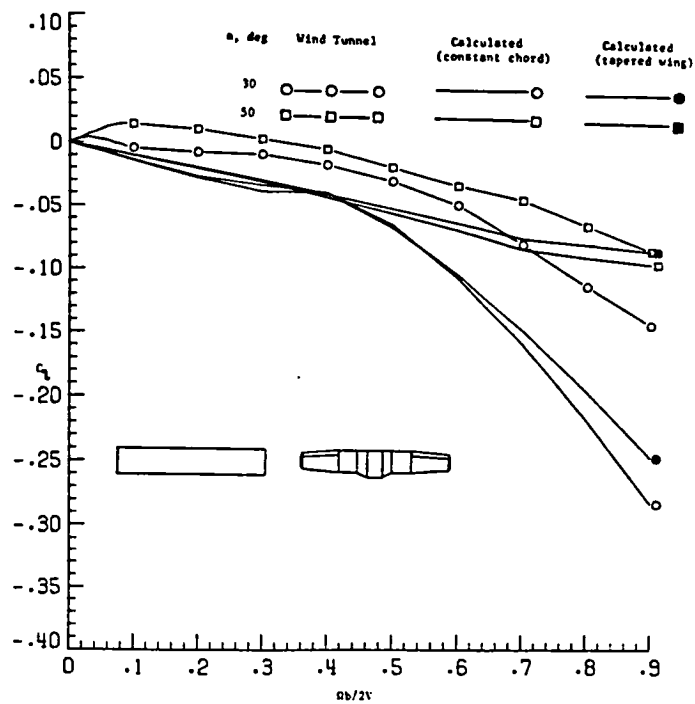
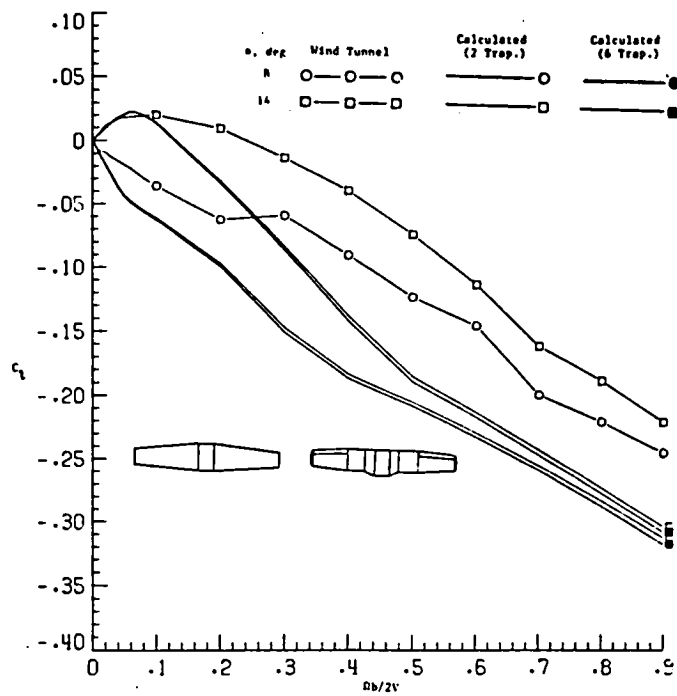


Figure 5. Effects of rotation rate on rolling moment coefficient for 8 and 14 degrees angle of attack.



1. Report No. NASA TM-86365		2. Government Accession No.		3. Recipient's Catalog No.	
4. Title and Subtitle  A METHOD FOR ESTIMATING THE ROLLING MOMENT DUE TO SPIN RATE FOR ARBITRARY PLANFORM WINGS				5. Report Date January 1985	
				6. Performing Organization Code 505-34-03-06	
7. Author(s)  William A. Poppen, Jr.				8. Performing Organization Report No.	
9. Performing Organization Name and Address  NASA Langley Research Center Hampton, VA 23665				10. Work Unit No.	
				11. Contract or Grant No.	
12. Sponsoring Agency Name and Address  National Aeronautics and Space Administration Washington, DC 20546				13. Type of Report and Period Covered Technical Memorandum	
				14. Sponsoring Agency Code	
15. Supplementary Notes					
16. Abstract  The application of aerodynamic theory for estimating the force and moments acting upon spinning airplanes is of interest. For example, strip theory has been used to generate estimates of the aerodynamic characteristics as a function of spin rate for wing-dominated configurations for angles of attack up to 90 degrees. This work, which had been limited to constant chord wings, is extended here to wings comprised of tapered segments. Comparison of the analytical predictions with rotary balance wind tunnel results shows that large discrepancies remain, particularly for those angles-of-attack greater than 40 degrees.					
17. Key Words (Suggested by Author(s))  Parameter Estimation Spin			18. Distribution Statement  Unclassified - Unlimited  Subject Category - 08		
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